

# SCMS Seminar



## ON THE SYLVESTER CONJECTURE

**Speaker: Dr. Shu Jie**

**SCMS**

**Time:** 9:30 -10:10, Thursday, June 29, 2017

**Venue:** Room 2201, East Guanghua Tower (Main), Fudan University

**Abstract:** A nonzero rational number is called a cube sum if it is of the form  $a^3+b^3$ , with  $a,b \in \mathbb{Q}^\times$ . To determine whether a rational number  $n$  is a cube sum is closely related to the arithmetic of the corresponding elliptic curve  $x^3 + y^3 = nz^3$ . A famous conjecture concerning the cube sums is the so-called Sylvester conjecture: Any prime congruent to  $4,7,8 \pmod{9}$  is a cube sum. Dasgupta and Voight proved certain primes  $4, 7 \pmod{9}$  are cube sums by establishing the nontriviality of certain related Heegner points. Based on the work of Dasgupta and Voight, we prove the Birch and Swinnerton-Dyer conjecture for the related elliptic curves by establishing the explicit Gross-Zagier formulae of the related Heegner points. This is a joint work with Hongbo Yin.